General Certificate of Education June 2007 Advanced Subsidiary Examination

MATHEMATICS Unit Pure Core 1

Monday 21 May 2007 9.00 am to 10.30 am

For this paper you must have:

• an 8-page answer book

• the **blue** AQA booklet of formulae and statistical tables. You must **not** use a calculator.

Time allowed: 1 hour 30 minutes

Instructions

- Use blue or black ink or ball-point pen. Pencil should only be used for drawing.
- Write the information required on the front of your answer book. The *Examining Body* for this paper is AQA. The *Paper Reference* is MPC1.
- Answer **all** questions.
- Show all necessary working; otherwise marks for method may be lost.
- The use of calculators (scientific and graphics) is **not** permitted.

Information

- The maximum mark for this paper is 75.
- The marks for questions are shown in brackets.

Advice

• Unless stated otherwise, you may quote formulae, without proof, from the booklet.



MPC1

Answer all questions.

- 1 The points A and B have coordinates (6, -1) and (2, 5) respectively.
 - (a) (i) Show that the gradient of AB is -3/2. (2 marks)
 (ii) Hence find an equation of the line AB, giving your answer in the form ax + by = c, where a, b and c are integers. (2 marks)
 - (b) (i) Find an equation of the line which passes through B and which is perpendicular to the line AB. (2 marks)
 - (ii) The point *C* has coordinates (*k*, 7) and angle *ABC* is a right angle.Find the value of the constant *k*. (2 marks)

2 (a) Express
$$\frac{\sqrt{63}}{3} + \frac{14}{\sqrt{7}}$$
 in the form $n\sqrt{7}$, where *n* is an integer. (3 marks)

(b) Express
$$\frac{\sqrt{7}+1}{\sqrt{7}-2}$$
 in the form $p\sqrt{7}+q$, where p and q are integers. (4 marks)

- 3 (a) (i) Express $x^2 + 10x + 19$ in the form $(x+p)^2 + q$, where p and q are integers. (2 marks)
 - (ii) Write down the coordinates of the vertex (minimum point) of the curve with equation $y = x^2 + 10x + 19$. (2 marks)
 - (iii) Write down the equation of the line of symmetry of the curve $y = x^2 + 10x + 19$. (1 mark)
 - (iv) Describe geometrically the transformation that maps the graph of $y = x^2$ onto the graph of $y = x^2 + 10x + 19$. (3 marks)
 - (b) Determine the coordinates of the points of intersection of the line y = x + 11 and the curve $y = x^2 + 10x + 19$. (4 marks)

4 A model helicopter takes off from a point O at time t = 0 and moves vertically so that its height, y cm, above O after time t seconds is given by

$$y = \frac{1}{4}t^4 - 26t^2 + 96t$$
, $0 \le t \le 4$

(a) Find:

(i)
$$\frac{dy}{dt}$$
; (3 marks)
(ii) $\frac{d^2y}{dt^2}$. (2 marks)

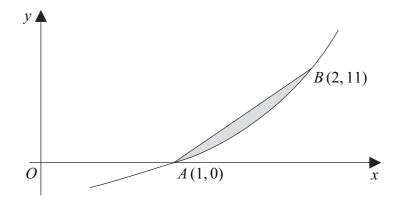
- (b) Verify that y has a stationary value when t = 2 and determine whether this stationary value is a maximum value or a minimum value. (4 marks)
- (c) Find the rate of change of y with respect to t when t = 1. (2 marks)
- (d) Determine whether the height of the helicopter above O is increasing or decreasing at the instant when t = 3. (2 marks)
- 5 A circle with centre C has equation $(x+3)^2 + (y-2)^2 = 25$.
 - (a) Write down:

(i) the coordinates of C; (2 m	arks)
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- (ii) the radius of the circle. (1 mark)
- (b) (i) Verify that the point N(0, -2) lies on the circle. (1 mark)
 - (ii) Sketch the circle. (2 marks)
 - (iii) Find an equation of the normal to the circle at the point N. (3 marks)
- (c) The point P has coordinates (2, 6).
 - (i) Find the distance *PC*, leaving your answer in surd form. (2 marks)
 - (ii) Find the length of a tangent drawn from P to the circle. (3 marks)

Turn over for the next question

- 6 (a) The polynomial f(x) is given by $f(x) = x^3 + 4x 5$.
 - (i) Use the Factor Theorem to show that x 1 is a factor of f(x). (2 marks)
 - (ii) Express f(x) in the form $(x-1)(x^2 + px + q)$, where p and q are integers. (2 marks)
 - (iii) Hence show that the equation f(x) = 0 has exactly one real root and state its value. (3 marks)
 - (b) The curve with equation $y = x^3 + 4x 5$ is sketched below.



The curve cuts the x-axis at the point A(1,0) and the point B(2,11) lies on the curve.

(i) Find
$$\int (x^3 + 4x - 5) dx$$
. (3 marks)

(ii) Hence find the area of the shaded region bounded by the curve and the line AB. (4 marks)

7 The quadratic equation

$$(2k-3)x^2 + 2x + (k-1) = 0$$

where k is a constant, has real roots.

- (a) Show that $2k^2 5k + 2 \le 0$. (3 marks)
- (b) (i) Factorise $2k^2 5k + 2$. (1 mark)
 - (ii) Hence, or otherwise, solve the quadratic inequality

$$2k^2 - 5k + 2 \leqslant 0 \tag{3 marks}$$

END OF QUESTIONS

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