

Centre Number						Candidate Number				
Surname										
Other Names										
Candidate Signature										

For Examiner's Use	
Examiner's Initials	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
TOTAL	



General Certificate of Education  
Advanced Subsidiary Examination  
January 2012

# Mathematics

# MPC1

## Unit Pure Core 1

Friday 13 January 2012 9.00 am to 10.30 am

<p><b>For this paper you must have:</b></p> <ul style="list-style-type: none"> <li>the blue AQA booklet of formulae and statistical tables.</li> </ul> <p>You must <b>not</b> use a calculator.</p>	
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### Time allowed

- 1 hour 30 minutes

### Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer the questions in the spaces provided. Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.
- The use of calculators is **not** permitted.

### Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

### Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.



J A N 1 2 M P C 1 0 1

Answer **all** questions in the spaces provided.

- 1** The point  $A$  has coordinates  $(6, -4)$  and the point  $B$  has coordinates  $(-2, 7)$ .
- (a)** Given that the point  $O$  has coordinates  $(0, 0)$ , show that the length of  $OA$  is less than the length of  $OB$ . *(3 marks)*
- (b) (i)** Find the gradient of  $AB$ . *(2 marks)*
- (ii)** Find an equation of the line  $AB$  in the form  $px + qy = r$ , where  $p$ ,  $q$  and  $r$  are integers. *(3 marks)*
- (c)** The point  $C$  has coordinates  $(k, 0)$ . The line  $AC$  is perpendicular to the line  $AB$ . Find the value of the constant  $k$ . *(3 marks)*

QUESTION  
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- 2 (a)** Factorise  $x^2 - 4x - 12$ . (1 mark)
- (b)** Sketch the graph with equation  $y = x^2 - 4x - 12$ , stating the values where the curve crosses the coordinate axes. (4 marks)
- (c) (i)** Express  $x^2 - 4x - 12$  in the form  $(x - p)^2 - q$ , where  $p$  and  $q$  are positive integers. (2 marks)
- (ii)** Hence find the minimum value of  $x^2 - 4x - 12$ . (1 mark)
- (d)** The curve with equation  $y = x^2 - 4x - 12$  is translated by the vector  $\begin{bmatrix} -3 \\ 2 \end{bmatrix}$ .  
Find an equation of the new curve. You need not simplify your answer. (2 marks)

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**3 (a) (i)** Simplify  $(3\sqrt{2})^2$ . (1 mark)

**(ii)** Show that  $(3\sqrt{2} - 1)^2 + (3 + \sqrt{2})^2$  is an integer and find its value. (4 marks)

**(b)** Express  $\frac{4\sqrt{5} - 7\sqrt{2}}{2\sqrt{5} + \sqrt{2}}$  in the form  $m - \sqrt{n}$ , where  $m$  and  $n$  are integers. (4 marks)

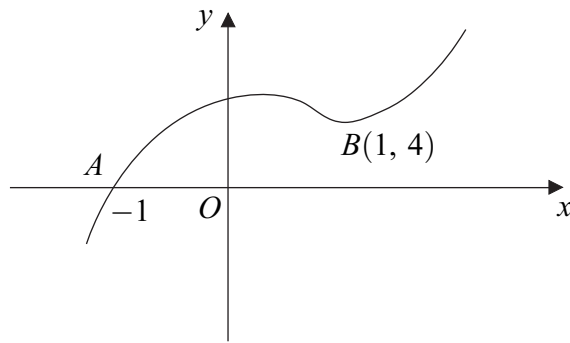
QUESTION  
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- 4 The curve with equation  $y = x^5 - 3x^2 + x + 5$  is sketched below. The point  $O$  is at the origin and the curve passes through the points  $A(-1, 0)$  and  $B(1, 4)$ .



(a) Given that  $y = x^5 - 3x^2 + x + 5$ , find:

(i)  $\frac{dy}{dx}$ ; (3 marks)

(ii)  $\frac{d^2y}{dx^2}$ . (1 mark)

(b) Find an equation of the tangent to the curve at the point  $A(-1, 0)$ . (2 marks)

(c) Verify that the point  $B$ , where  $x = 1$ , is a minimum point of the curve. (3 marks)

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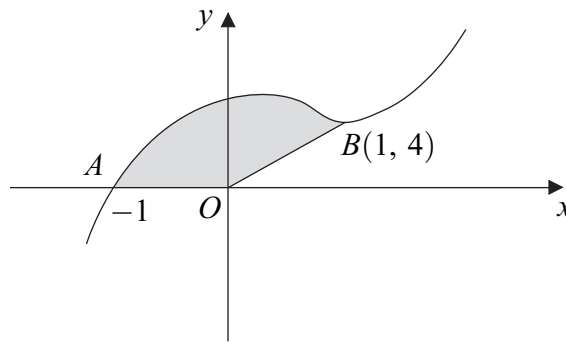
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**4 (d)** The curve with equation  $y = x^5 - 3x^2 + x + 5$  is sketched below. The point  $O$  is at the origin and the curve passes through the points  $A(-1, 0)$  and  $B(1, 4)$ .



(i) Find  $\int_{-1}^1 (x^5 - 3x^2 + x + 5) dx$ . (5 marks)

(ii) Hence find the area of the shaded region bounded by the curve between  $A$  and  $B$  and the line segments  $AO$  and  $OB$ . (2 marks)

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- 6** A rectangular garden is to have width  $x$  metres and length  $(x + 4)$  metres.
- (a)** The perimeter of the garden needs to be greater than 30 metres.  
Show that  $2x > 11$ . *(1 mark)*
- (b)** The area of the garden needs to be less than 96 square metres.  
Show that  $x^2 + 4x - 96 < 0$ . *(1 mark)*
- (c)** Solve the inequality  $x^2 + 4x - 96 < 0$ . *(4 marks)*
- (d)** Hence determine the possible values of the width of the garden. *(1 mark)*

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**7** A circle with centre  $C$  has equation  $x^2 + y^2 + 14x - 10y + 49 = 0$ .

**(a)** Express this equation in the form

$$(x - a)^2 + (y - b)^2 = r^2 \qquad \qquad (3 \text{ marks})$$

**(b)** Write down:

**(i)** the coordinates of  $C$  ;

**(ii)** the radius of the circle. (2 marks)

**(c)** Sketch the circle. (2 marks)

**(d)** A line has equation  $y = kx + 6$ , where  $k$  is a constant.

**(i)** Show that the  $x$ -coordinates of any points of intersection of the line and the circle satisfy the equation  $(k^2 + 1)x^2 + 2(k + 7)x + 25 = 0$ . (2 marks)

**(ii)** The equation  $(k^2 + 1)x^2 + 2(k + 7)x + 25 = 0$  has equal roots. Show that

$$12k^2 - 7k - 12 = 0 \qquad \qquad (3 \text{ marks})$$

**(iii)** Hence find the values of  $k$  for which the line is a tangent to the circle. (2 marks)

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